
Pushover Analysis of a RC Building Resting on Sloping Ground

¹Nitin Jain and ²Goutam Ghosh

^{1,2}Motilal Nehru National Institute of Technology Allahabad, Prayagraj-211004, UP, India

¹ nitin.jain041995@gmail.com, ² goutam@mnnit.ac.in

Abstract

Several past earthquakes study suggest that earthquake have had a significant impact on the network system as well as considerable catastrophic effects on human life, buildings, bridges and economy. Hilly buildings are more susceptible to severe damage under lateral forces (earthquake ground motion) as compared to buildings in plains, as they are irregular and unsymmetrical in horizontal and vertical planes and torsionally coupled. Past earthquakes like Kangra (1950), Tokachi-Oki-Japan(1968) and Uttarkashi-India(1991) have proved that the buildings located near the edge of stretch of hills or sloping ground suffered severe damages. In this paper, the seismic behaviour of a G+4 Reinforced Concrete (RC) building is being compared considering two conditions viz. (i) resting on plain terrain and (ii) resting on sloping ground. The seismic design of the building has been performed as per IS 1893 (Part I): 2016 and the ductile detailing provisions have been considered as per IS 13920: 2016. The modelling and analysis of the buildings have been done in ETABS. Plastic hinges have been assigned to the frame elements to incorporate the nonlinear behaviour. A nonlinear static pushover analysis has been performed for the buildings and the capacity curve and ductility demand have been determined. It has been observed that there is a change in the dynamic characteristics and increase in the vulnerability along with variation in ductility demand of the buildings resting on slope. The results obtained from the present study will help in evaluating the seismic performance and risk of failure of the hilly buildings.

Keywords. RC building; pushover; ductility; seismic; performance.

1. INTRODUCTION

The rapid urbanization and economic growth in hilly region has accelerated the real estate development, as an impact of this population density increased enormously in hilly region, which leads to the construction of multi-storeyed buildings on sloping ground [1]. The scarcity of plain terrain compels the construction activities to be done on sloping ground [2]. Varied configurations of buildings in hilly areas results the buildings to be highly irregular and asymmetric, due to the variation in mass and stiffness distributions on different vertical axis at each floor [3,4]. In this study the main focus is the comparison of the seismic behaviour of a G+4 RC building having two different conditions viz. (i) resting on plain terrain and (ii) resting on sloping ground [6]. All the seismic design considerations are being considered as per the IS 1893 (Part I) [5]: 2016 and the ductile detailing provisions have been considered as per IS 13920: 2016 [7]. The modelling and analysis of the buildings have

been done in ETABS [10]. Models are being compared on the basis of their time periods, mass participation ratios, base shear, column forces, storey drifts, capacity curve and ductility demand [8,9,11]. The results obtained from the present study will help in evaluating the seismic performance of the hilly buildings.

2. OBJECTIVES OF WORK

- To study the comparison of the seismic behaviour of a G+4 RC building having two different conditions viz. (i) resting on plain terrain and (ii) resting on sloping ground on the basis of their time periods, mass participation ratios, base shear, column forces, storey drifts.
- A nonlinear static pushover analysis has been performed for the different models and the capacity curves and ductility demands have been determined.

3. DESCRIPTION OF BUILDING

| | |
|--|---|
| Plan area- 16m X 16m | Number of storey-5 |
| Height of bottom story- 4m and all other stories- 3m | Total height of building- 16m |
| Cross-section of the column- 300mm X 300mm | Cross-section of the beam- 230mm X 300mm |
| Thickness of the slab- 150mm | Grade of Concrete- M25 |
| Grade of Steel- HYSD500 | Weight density of brick - 20kN/m ³ |
| Roof Live load- 1.5kN/m ² | Live load- 3kN/m ² |
| Sloping ground angle-15° | |

SEISMIC DATA

| | |
|------------------------------|-----------------------------|
| Seismic zone-V | Zone factor-0.36 |
| Importance factor-1 | Response reduction factor-5 |
| Function damping ratio- 0.05 | Soil type- II (Medium Soil) |

4. MODELLING

MODEL 1: G+4 Reinforced Concrete (RC) building resting on plain terrain. (Figure 1)

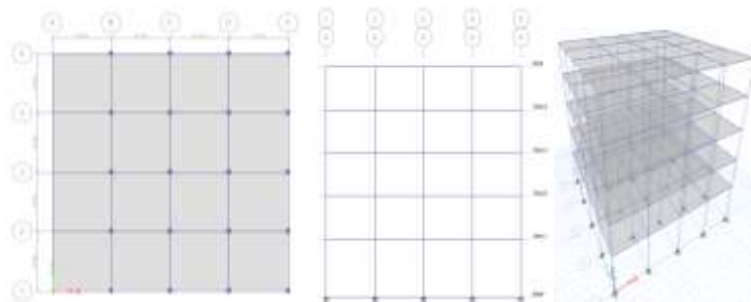


Figure 1. Plan, Elevation and 3D (Model 1)

MODEL 2: G+4 Reinforced Concrete (RC) building resting on sloping ground with one extra slab at the plinth level so that the space can be utilized (Figure 2).

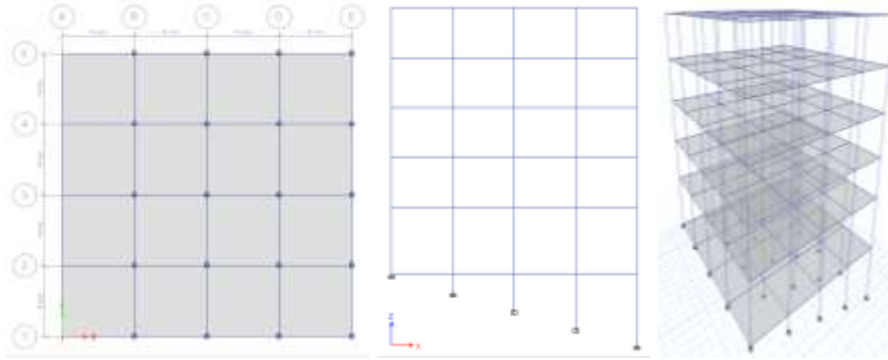


Figure 2. Plan, Elevation and 3D (Model 2)

5. ANALYSIS AND RESULTS

5.1. Time Period

Building acts as an inverted pendulum and has been considered as lumped mass system. One lumped mass get increased with increase in the storey. When earthquake occur building start vibrating under forced vibration and when earthquake completes then building vibrates as free vibration and vibrates at natural frequency. The time required to complete one complete cycle of oscillation when it was disturbed and left free is called natural time period. Natural time period is inverse of natural frequency. It depends on mass and stiffness of the building. Time period for Model 1 and Model 2 is presented in Table 1.

$$T_n = 2\pi\sqrt{m/k}$$

Table 1. Time period for model 1 and model 2

| Mode | Time Period(sec) | |
|------|------------------|---------|
| | Model 1 | Model 2 |
| 1 | 1.124 | 1.58 |
| 2 | 1.124 | 1.578 |
| 3 | 0.984 | 1.397 |
| 4 | 0.354 | 0.492 |
| 5 | 0.354 | 0.491 |
| 6 | 0.311 | 0.437 |

5.2. Mass Participation Ratio

The percent of structural mass that is participating in a given direction and mode is known as the mass participation ratio. The ration for Model 1 and Model 2 is given in Table 2 and 3 respectively.

Table 2. Mass participation ratios for model 1

| Mode | UX | UY | RZ |
|------|------------|------------|--------|
| 1 | 0.894 | 0.00001354 | 0 |
| 2 | 0.00001354 | 0.894 | 0 |
| 3 | 0 | 0 | 0.8958 |
| 4 | 0.0805 | 0.00001162 | 0 |
| 5 | 0.00001162 | 0.0805 | 0 |
| 6 | 0 | 0 | 0.0794 |

Table 3. Mass participation ratios for model

| Mode | UX | UY | RZ |
|------|-------------|--------|------------|
| 1 | 0.0075 | 0.893 | 0.0088 |
| 2 | 0.9017 | 0.0075 | 0.00000429 |
| 3 | 0.00004003 | 0.0086 | 0.9011 |
| 4 | 0.0021 | 0.0688 | 0.0002 |
| 5 | 0.0692 | 0.0021 | 0 |
| 6 | 0.000004542 | 0.0005 | 0.0705 |

5.3. Base Shear

The total amount of shear acting in a lateral direction on all the storeys of a building is known as the Base Shear of the building. Base shear plays a crucial role while selecting the type of foundation. Stronger foundations are required when the base shear of a building is as high as compared to low base shear. The following expression is used for the calculation of base shear:

$$V_b = A_h \times W$$

Where A_h = Design horizontal seismic coefficient for structure.

W = Seismic weight of the building.

Table 4. Base shear for model 1 and model 2

| Model | Base Shear | |
|---------|------------------|------------------|
| | X-direction (kN) | Y-direction (kN) |
| Model 1 | 468.65 | 468.65 |
| Model 2 | 240.64 | 238.13 |

5.4. Column Forces

Comparison of forces on 5 exterior columns of both the models is presented in Table 5.

Table 5. Column forces in exterior columns of model 1 and model 2

| Column n | Model 1 | | | Model 2 | | |
|-------------|-----------|--------------------------|--------------------------|-----------|--------------------------|--------------------------|
| | P (kN) | M ₂ (kN-m) | M ₃ (kN-m) | P (kN) | M ₂ (kN-m) | M ₃ (kN-m) |
| 1 | 334.7348 | 46.137 | 46.7623 | 342.7071 | 51.1434 | 58.0688 |
| 2 | 611.6728 | 44.2977 | 57.172 | 810.923 | 38.466 | 23.2983 |
| 3 | 609.6403 | 44.3312 | 56.4659 | 818.2662 | 41.7977 | 20.6865 |
| 4 | 607.8509 | 44.4752 | 56.8283 | 820.5263 | 38.5937 | 17.6855 |
| 5 | 334.7239 | 46.4941 | 53.8438 | 443.8706 | 31.4064 | 15.9027 |

5.5. Storey Drift

As we have discussed in this paper, the building acts as a spring mass system. In which the floor level acts as a mass and the columns impart stiffness to the structure. When a seismic load acts on the structure, each mass vibrates differently depending on the location and amount of its mass value. The relative displacement between two adjacent storeys is known as storey drift. Storey drift for Model 1 when response spectrum in X and Y-direction is presented in Figure 3 and Table 6 and in Figure 4 and Table 7 respectively. Storey drift for Model 2 when response spectrum in X and Y-direction is presented in Figure 5 and Table 8 and in Figure 6 and Table 9 respectively.

For Model 1

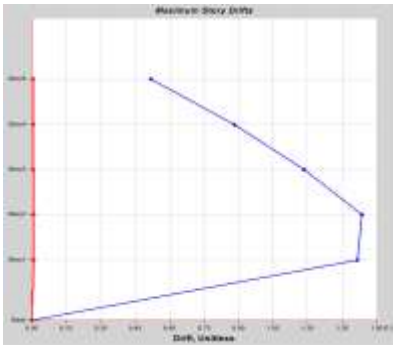


Figure 3. Storey drift for model 1 when response spectrum in X-direction

| Storey | Elevation | Location | X-Dir | Y-Dir |
|---------|-----------|----------|----------|----------|
| | M | | | |
| Roof | 16 | Top | 0.000518 | 0.000008 |
| Storey4 | 13 | Top | 0.000882 | 0.000008 |
| Storey3 | 10 | Top | 0.001185 | 0.000007 |
| Storey2 | 7 | Top | 0.001434 | 0.000001 |
| Story1 | 4 | Top | 0.001415 | 0.000009 |
| Base | 0 | Top | 0 | 0 |

Table 6. Storey drift values for model 1 when response spectrum in X-direction

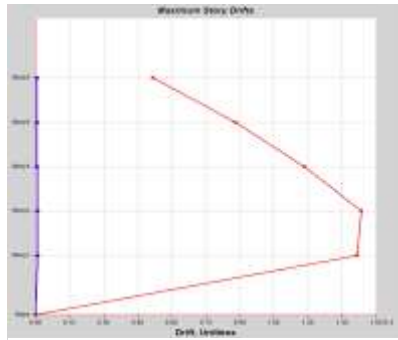


Figure 4. Storey drift for model 1 when response spectrum in Y-direction

| Story | Elevation | Location | X-Dir | Y-Dir |
|----------|-----------|----------|----------|----------|
| M | | | | |
| Roof | 16 | Top | 0.000008 | 0.000518 |
| Story4 | 13 | Top | 0.000008 | 0.000882 |
| Story3 | 10 | Top | 0.000007 | 0.001185 |
| Story2 | 7 | Top | 0.00001 | 0.001434 |
| Story1 | 4 | Top | 0.000009 | 0.001415 |
| Base | 0 | Top | 0 | 0 |

Table 7. Storey drift values for model 1 when response spectrum in Y-direction

For Model 2

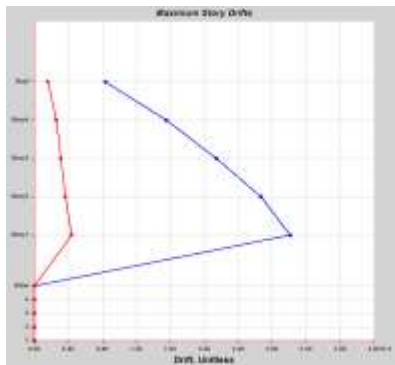


Figure 5. Storey drift for model 2 when response spectrum in X-direction

| Storey | Elevation | Location | X-Dir | Y-Dir |
|----------|-----------|----------|----------|----------|
| M | | | | |
| Roof | 20.288 | Top | 0.000833 | 0.00016 |
| Storey4 | 17.288 | Top | 0.001553 | 0.000259 |
| Storey3 | 14.288 | Top | 0.002142 | 0.000312 |
| Storey2 | 11.288 | Top | 0.002668 | 0.000364 |
| Storey1 | 8.288 | Top | 0.003011 | 0.000441 |
| Base | 4.288 | Top | 0 | 0 |
| 4 | 3.216 | Top | 0 | 0 |
| 3 | 2.144 | Top | 0 | 0 |
| 2 | 1.072 | Top | 0 | 0 |
| 1 | 0 | Top | 0 | 0 |

Table 8. Storey drift values for model 2 when response spectrum in X-direction

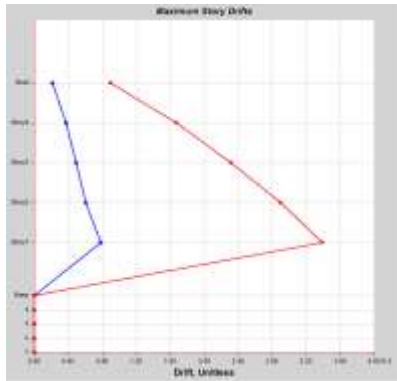


Figure 6. Storey drift for model 2 when response spectrum in Y-direction

| Storey | Elevation | Location | X-Dir | Y-Dir |
|----------|-----------|----------|----------|----------|
| M | | | | |
| Roof | 20.288 | Top | 0.000214 | 0.000895 |
| Storey4 | 17.288 | Top | 0.000374 | 0.001674 |
| Storey3 | 14.288 | Top | 0.000489 | 0.002316 |
| Storey2 | 11.288 | Top | 0.000602 | 0.002897 |
| Storey1 | 8.288 | Top | 0.000785 | 0.003388 |
| Base | 4.288 | Top | 0 | 0 |
| 4 | 3.216 | Top | 0 | 0 |
| 3 | 2.144 | Top | 0 | 0 |
| 2 | 1.072 | Top | 0 | 0 |
| 1 | 0 | Top | 0 | 0 |

Table 9. Storey drift values for model 2 when response spectrum in Y-direction

5.6. Capacity Curve

The non-linear behaviour of the structure can be shown by the Capacity Curve or Pushover Curve. It is the load deformation curve of the base shear and the horizontal roof displacement of the building. Capacity curve for model 1 when response spectrum in X and Y-direction is presented in Figure 7 and 8 respectively. Capacity curve for model 2 when response spectrum in X and Y-direction is presented in Figure 9 and 10 respectively.

For Model 1

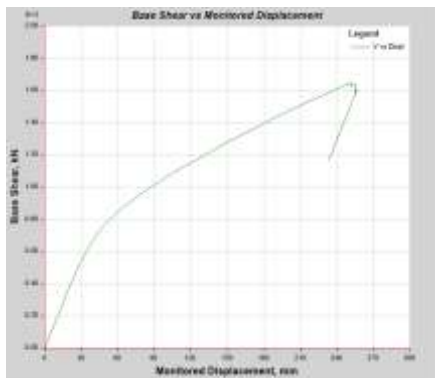


Figure 7. Capacity Curve for model 1 when response spectrum in X-direction

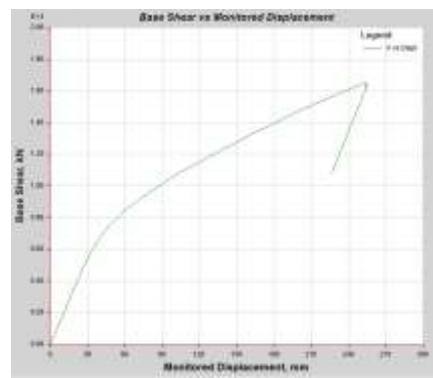


Figure 8. Capacity Curve for model 1 when response spectrum in Y-direction

For Model 2

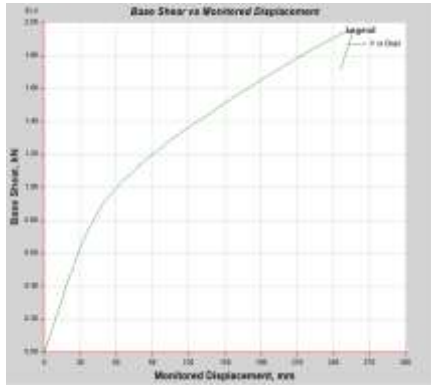


Figure 9. Capacity Curve for model 2 when response spectrum in X-direction

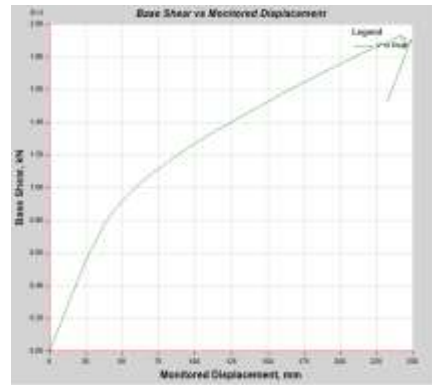


Figure 10. Capacity Curve for model 2 when response spectrum in Y-direction

5.7. Performance Point

The intersection point between the capacity spectrum and the demand spectrum at a given damping ratio is termed the Performance Point. It is the maximum inelastic capacity of the structure. Performance point for model 1 when pushover analysis in X and Y direction is presented in Figure 11 and 12 respectively and for module 2 is presented in Figure 13 and 14 respectively.

For Model 1

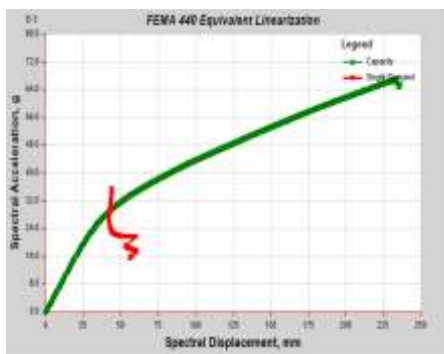
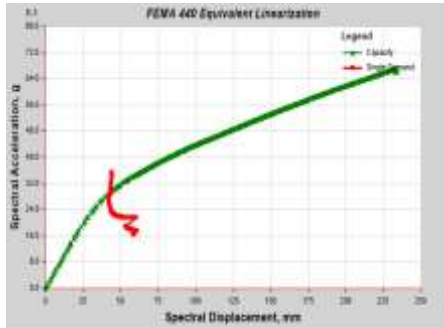


Figure 11. Performance point for model 1 when pushover analysis in X-direction

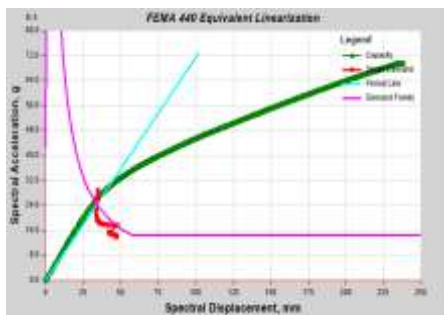
| | | | |
|--------------------|-------------|---------------------|-----------------|
| Point Found | Yes | T secant | 2.43 sec |
| Shear | 740.7828 kN | T effective | 2.407 sec |
| Displacement | 46.634 mm | Ductility Ratio | 1.668543 |
| Sa | 0.029309 | Effective Damping | 0.0686 |
| Sd | 42.991 mm | Modification Factor | 0.980907 |



| | | | |
|--------------------|-------------|---------------------|-----------------|
| Point Found | Yes | T secant | 2.43 sec |
| Shear | 743.2573 kN | T effective | 2.409 sec |
| Displacement | 46.688 mm | Ductility Ratio | 1.672114 |
| Sa | 0.029313 | Effective Damping | 0.0688 |
| Sd | 43.015 mm | Modification Factor | 0.982096 |

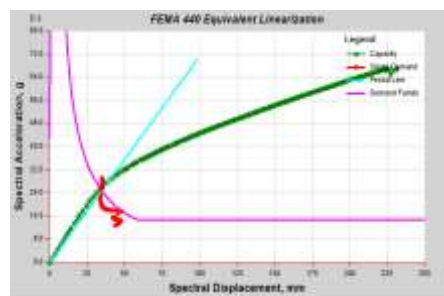
Figure 12. Performance point for model 1 when pushover analysis in Y-direction

For Model 2



| | | | |
|--------------------|-------------|---------------------|------------------|
| Point Found | Yes | T secant | 2.305 sec |
| Shear | 756.6875 kN | T effective | 2.316 sec |
| Displacement | 37.443 mm | Ductility Ratio | 1.519953 |
| Sa | 0.026431 | Effective Damping | 0.0617 |
| Sd | 34.873 mm | Modification Factor | 1.00973 |

Figure 13. Performance point for model 2 when pushover analysis in X-direction



| | | | |
|--------------------|------------|-----------------|------------------|
| Point Found | Yes | T secant | 2.323 sec |
| Shear | 770.4671 | T effective | 2.335 sec |
| Displacement | 37.701 | Ductility Ratio | 1.567648 |
| Sa | 0.025992 | Effective | 0.0638 |
| Sd | 34.843 | Modification | 1.010133 |

Figure 14. Performance point for model 2 when pushover analysis in Y-direction

6. CONCLUSION

In the present paper, the seismic analysis of a G+4 Reinforced Concrete (RC) building has been done considering the building is resting on plain and hilly terrains. The seismic design of the building has been performed as per IS 1893 (Part I): 2016 and the ductile detailing provisions have been considered as per IS 13920: 2016. The following conclusions can be drawn. A. The time period of the building resting on hilly slope is found to be higher than the same resting on plain ground which might be due to additional flexibility because of unsymmetrical configuration in the former case. B. The base shear for the hilly building is found to be lesser than the same resting on plain ground which might be due to increased flexibility in the former case. C. The storey drift is found to be higher in case of hilly terrain building than the building resting on plain ground. However, for both the buildings, the drifts are within the desired limit as per IS:1893-2016 code. D. The ductility demand of the building resting on hilly terrain is higher than the same resting on plain ground which might be due to unsymmetrical configuration in the former case.

REFERENCES

- [1] R. B. Khadiranaikar and A. Masali, "Seismic Performance of Buildings Resting on Sloping Ground," *Advances in Structural Engineering*, pp. 803–813, Dec. 2014, doi: 10.1007/978-81-322-2193-7_63.
- [2] S. Goyal. Dynamic Analysis of Sloped Buildings: Experimental and Numerical Studies (Doctoral dissertation), 2015. [Online], Available: http://ethesis.nitrkl.ac.in/6801/1/DYNAMIC_Goyal_2015.pdf
- [3] Z. Mohammad, A. Baqi, and M. Arif, "Seismic Response of RC Framed Buildings Resting on Hill Slopes," *Procedia Engineering*, vol. 173, pp. 1792–1799, 2017, doi: 10.1016/j.proeng.2016.12.221.
- [4] IS: 456:2000 Plain and Reinforced Concrete-Code of Practice by Bureau of Indian Standards, 2000. [Online], Available: <https://archive.org/details/gov.in.is.456.2000>
- [5] IS: 1893(Part-1):2016 Criteria for Earthquake Resistant Design of Structures by Bureau of Indian Standards, 2016. [Online], Available: <https://www.studocu.com/in/document/birla-institute-of-technology-and-science-pilani/foundation-engineering/1893-part-1-2016-criteria-for-earthquake-resistant-design-of-structures-is-code-1893/9255021>
- [6] IS: 875 (Part 2) - 1987, Code of Practice Design Loads (Other Than for Earthquake) For Buildings and Structures by Bureau of Indian Standards, [Online], Available. <https://law.resource.org/pub/in/bis/S03/is.875.2.1987.pdf>
- [7] IS: 13920:2016 Ductile Design and Detailing of Reinforced Concrete Structures Subjected to Seismic Forces- Code of Practice by Bureau of Indian Standards, 2016. [Online], Available. <https://idoc.pub/documents/13920-2016-vlr0k1ryxjz>
- [8] FEMA-440: Improvement of Nonlinear Static Seismic Analysis Procedures June, 2005. [Online], Available. <https://mitigation.eeri.org/resource-library/building-professionals/improvement-of-nonlinear-static-seismic-analysis-procedures-fema-440>
- [9] ASCE/SEI 41-17(2017): Seismic Rehabilitation of Existing Buildings (ASCE/SEI 41-17). [Online], Available. <https://ascelibrary.org/doi/pdf/10.1061/9780784414859.fm>
- [10] ETABS 2017- Building Analysis and Design- Computers & Structures, Inc., Berkley, CA, USA. [Online], Available. <https://www.csiamerica.com/products/etabs>

- [11] D. E. Hudson, "Dynamics of structures: Theory and applications to earthquake engineering, by Anil K. Chopra, Prentice-Hall, Englewood Cliffs, NJ, 1995. No. of pages: xxviii + 761, ISBN 0-13-855214-2," Earthquake Engineering & Structural Dynamics, vol. 24, no. 8, pp. 1173–1173, Aug. 1995, doi: 10.1002/eqe.4290240809.

Biographies



Mr Nitin Jain is a Ph.D student in the Civil Engineering Department, MNNIT Allahabad, Prayagraj, India. He did his M.Tech. in Structural Engineering from IET Lucknow. His present area of research is Seismic performance evaluation of building structures.



Dr Goutam Ghosh, is currently an Associate Professor in the Civil Engineering Department, MNNIT Allahabad, Prayagraj, India. He did his Ph.D. from IIT Roorkee in the area of seismic performance of bridge structures. He has more than 15 years of teaching experience and has published several research papers in reputed Journals/Conferences. His area of interest is earthquake engineering, performance-based design of structures, base isolation of structures and bridge engineering.